



Meeting Point »Early Mathematics Education«  
Scientific Direction: Prof. Dr. Inge Schwank

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**Cherishing Children in their Mathematical Talent**  
**- Collection of Olympic Tasks -**

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